A time-dependent order parameter for ultrafast photoinduced phase transitions

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Strongly correlated electron systems often exhibit very strong interactions between structural and electronic degrees of freedom that lead to complex and interesting phase diagrams¹². For technological applications of these materials it is important to learn how to drive transitions from one phase to another. A key question here is the ultimate speed of such phase transitions, and to understand how a phase transition evolves in the time domain³⁻¹⁰. Here we apply time-resolved X-ray diffraction to directly measure the changes in long-range order during ultrafast melting of the charge and orbital ordered phase in a perovskite manganite. We find that although the actual change in crystal symmetry associated with this transition occurs over different timescales characteristic of the many electronic and vibrational coordinates of the system, the dynamics of the phase transformation can be well described using a single time-dependent ‘order parameter’ that depends exclusively on the electronic excitation.

The concept of an order parameter was introduced by Landau and Lifshitz to characterize phase transitions in the adiabatic limit¹⁴. Typically, a phase transition is characterized by a change of the order parameter from zero to a non-zero finite value as a function of a slowly changing thermodynamic state variable. The order parameter is a measure of symmetry breaking in the equilibrium state. The Landau free energy $F(\eta)$ is a phenomenological expression of the free energy of a system at a fixed value of the order parameter $\eta$. Near the phase transition, $\eta$ is small, allowing $F(\eta)$ to be approximated by the first terms of a Taylor expansion in $\eta$. The equilibrium value of the order parameter $\eta$ is given by the minimum of $F(\eta)$. Assuming simple relations between thermodynamic state variables and the Taylor coefficients provides a highly useful description of many types of commonly encountered phase transitions.

In real physical situations we rarely have the possibility of making truly adiabatic changes to induce phase transitions. An extreme example is the so-called ‘ultrafast’ phase transition, where a persistent symmetry change is induced by a sudden impulsive interaction from a laser pulse lasting only a few femtoseconds¹⁻¹¹. In this case, different coordinates of the phase transformation, that in equilibrium are tightly linked to the conventionally defined order parameter, can undergo quite different dynamics. Whether a unified explanation of such dynamics exists remains an open question.

To address this issue, we investigated the dynamics of the ultrafast phase transition in an epitaxially grown film of Pr₀.₅Ca₀.₅MnO₃ (PCMO), a perovskite-type manganite, a class of systems which exhibits properties such as colossal magnetoresistance and insulator-to-metal transitions that are intrinsically related to symmetry changes of the atomic lattice and to intriguing ordering patterns of the spins, orbitals and charges¹⁻¹⁵. Although much progress has been made in understanding the various schemes of magnetic, charge and orbital ordering and their relationship to the lattice, comparatively little is known about the interactions among these different degrees of freedom. Investigations of photoexcited manganites using optical probes suggest that the electronic properties change on a timescale faster than the period of the Jahn–Teller mode of 70 fs (refs 4,16). Complementary to optical probes, diffraction techniques yield a direct and quantitative measurement of the long-range order⁶,¹⁰,¹¹,¹³. Employing femtosecond X-ray diffraction (XRD) it has been shown that the change of lattice symmetry occurs on a slower but still sub-picosecond timescale⁶,¹⁷. Here we employ femtosecond XRD, which when tuned to a resonance offers, in addition to the lattice dynamics, information on the long-range charge and orbital order (COO; ref. 18). Taking advantage of the high X-ray flux of a free-electron laser (FEL; ref. 19) we are able to measure different classes of superlattice reflections, each sensitive to a specific component of the phase transition. We classify these into three categories (in Pbnm notation with k odd): one type of reflection $(0 k / 2 0)$ is sensitive directly to the orbital order and Jahn–Teller distortion, a second type $(0 k 0)$ is more sensitive to the charge order, and a general type $(h k / 2 l)$ measures predominantly the overall structural distortion¹⁸. Figure 1a shows a schematic of the optical-pump X-ray-probe experiment. Experimental details are given in the Methods. 1.55 eV photons mainly excite the Mn³⁺ intra-site transition²⁰, which drives the relaxation of the Jahn–Teller distortion (Fig. 1b,c).

Time-resolved XRD data for various reflections are shown in Fig. 2a–c. The observed dynamics for lower pump fluences are dominated by a strong 2.45 THz oscillation, which is the slowest of a series of coherent optical phonon modes observed when these materials are excited with very short optical pulses¹¹. Faster components can be inferred from the changes observed at early times, although the time resolution is insufficient to resolve them. At late times, the disappearance of the superlattice reflections

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Figure 1 | Ultrafast melting of charge and orbital order. a, Schematic set-up of the optical-pump/X-ray-probe experiment. In the asymmetric diffraction configuration the sample is rotated by an angle $\phi$ around its surface normal $s$ to fulfil the Bragg condition for a given reflection ($h \, k \, l$). CSPAD, Cornell-SLAC hybrid Pixel Array Detector\(^{29}\); PCMO, Pr\(_{0.5}\)Ca\(_{0.5}\)MnO\(_3\). b, In the cubic crystal field the degenerate Mn\(^{3+}\) 3\,d states are split into the $e_g$ and $t_{2g}$ bands. In the ground state, distortions of the oxygen octahedra at the Mn\(^{3+}\) sites further split the bands (Jahn–Teller effect). c, On cooling to the ground state charge and orbital order is observed alongside with a Jahn–Teller distortion of the Mn\(^{3+}\)O\(_6\) octahedra, leading to a doubling of the unit cell along the $b$ axis and a symmetry change from orthorhombic Pbnm to monoclinic $P2_1/m$ (ref. 30). The staggered configuration of the Mn\(^{3+}\) sites along $b$ is accompanied by the ordering of the elongated Mn\(^{3+}\) 3\,d\,$3z^2−r^2$ orbitals\(^{15}\). The black arrows show the motion of the Jahn–Teller mode for one Mn\(^{3+}/\)Mn\(^{4+}\) pair.

Figure 2 | Measured (top) and simulated (bottom) evolution of the normalized diffracted X-ray intensity for three superlattice reflections. a, d, The (2\,1/2\,0) reflection off resonance at 6.53 keV, which is sensitive only to the structural atomic motion. b, e, The (0\,5/2\,0) reflection is only slightly enhanced by $\sim$15% at resonance (6.553 keV) and therefore mainly sensitive to the Jahn–Teller distortion. c, f, The (0\,3\,0) reflection at 6.555 keV is strongly resonantly enhanced by a factor of $\sim$4 and mainly sensitive to the electronic order. The fluence required to suppress the Bragg peaks varies for the different reflections simply because of the birefringence of the material (Supplementary Information). The model used to generate the simulated curves d–f is discussed in the manuscript.

At high pump fluences is unambiguous evidence that the lattice symmetry has changed. Even before this, the observed doubling of the oscillation frequency in the diffracted signal is evidence of another kind of symmetry change in the potential energy surface: the atoms coherently oscillate with a frequency of $\sim$2.45 THz over the equilibrium positions of a higher-symmetry lattice. These oscillations persist for a short time before the coherent motions relax and the phase transition is completed.

To gain a better understanding of the fluence dependent dynamics we first discuss the behaviour of the (0\,3\,0) reflection (Fig. 2c), which at resonance is predominantly a measure of the charge order. If we assume that the purely electronic degrees of freedom...
freedom thermalize within our time resolution, we can define an effective ‘time-dependent order parameter’ \( \eta \) that gives a measure of the symmetry breaking of the electronic system at a particular time \( t \). We can therefore identify \( \eta \) with the structure factor \( F^{\rho(3)} \) of the (030) reflection.

Within the accuracy of the experiment we find that the diffracted X-ray intensity \( I^{\rho(3)} = |F^{\rho(3)}|^2 \) averaged in the 250–500 fs time interval drops linearly with fluence until it vanishes at \( \sim 4 \text{ mJ cm}^{-2} \) (Fig. 3, red curve). At 250–500 fs after excitation we then have \( \eta_i = \sqrt{1 - n_i/n_c} \) for an absorbed energy density \( n_i \) less than a critical energy density \( n_c \). Here we have normalized \( \eta \) to unity at times before excitation. For \( n_i > n_c \) the phase transition takes place and \( \eta = 0 \). The optical absorption length at 800 nm is on the order of the film thickness. To quantitatively describe the fluence-dependent data we account for the inhomogeneity of the excitation \( n_i(z) \) by dividing the film into \( N \) slices along the depth \( z \) (Supplementary Information) and compute the structure factor \( F^{\rho(3)} = 1/N \sum_i \eta_i(z) \).

For \( n_i < n_c \) the fast change in electronic order induced by the excitation pulse partially recovers within a few picoseconds (Fig. 2c), reaching a quasi-equilibrium state empirically well described by \( \eta_i = (1 - n_i/n_c)^2 \) (Fig. 3, blue curve). The observed recovery of charge order may be attributed to energy transfer from the initially excited electron system to the lattice. Generalizing the relation between \( \eta \) and \( n_i \), we find above a definition of a time-dependent order parameter:

\[
\eta_i(t) = \sqrt{1 - n_i(t)/n_c}
\]

For \( n_i < n_c \) we can then empirically describe the evolving electronic energy density by

\[
n_i(t) = (n_i - \alpha n_i) e^{-t/\tau} + \alpha n_c \tag{2}\]

with \( \alpha = 1 - (1 - n_i/n_c)^2 \). Here \( \tau \) is an effective relaxation time and \( \gamma \) is analogous to a critical exponent of the initial excitation. A fit to the (030) intensity based on equations (1) and (2) is superimposed on the data in the inset of Fig. 3, yielding \( \gamma = 0.21(1), \tau = 0.81(4) \text{ ps} \) and \( n_c = 477(7) \text{ cm}^{-2} \) (\( \approx 1.33 \text{ eV per unit cell} \)).

The full phase transition requires not only a symmetry change in the charge distribution, but also a motion of the atoms to a higher-symmetry site position that is coherently driven by electronic excitation via a fast change of the atomic potential\(^{23,24,25}\). Here the rapid laser-induced melting of charge and orbital order releases the forces that stabilize the Jahn–Teller lattice distortions at the Mn\(^{2+}\) sites\(^{23,24,25}\). This sudden release of force triggers a chain reaction that couples to other vibrational modes, leading to a rearrangement of the atoms in the unit cell.

The timescales of this atomic motion are determined by the eigenmodes of the lattice\(^{23,24,25}\). In Fig. 2a, we clearly see that the dynamics involve oscillatory motions around a quasi-equilibrium position. In view of the complicated atomic structure of PCMO and our limited knowledge of the eigenmodes, an exact treatment of the structural dynamics is not feasible. In our model we approximate the atomic motions relevant to the phase transition to four groups of effective modes and we make the following ansatz for the time-dependent atomic potential:

\[
V(t) = -\frac{a}{2} \left(1 - \frac{n_i(t)}{n_c}\right) \nu_1^2 + \frac{b}{4} \nu_2^4 + \frac{c_{\nu_1}}{2} \left(\nu_2 - \nu_1\right)^2 + \frac{c_{\nu_2}}{2} \left(\nu_3 - \nu_2\right)^2 + \frac{c_{\nu_3}}{2} \left(\nu_4 - \nu_3\right)^2 \tag{3}\]

Here \( \nu \) are atomic motion coordinates relevant to the structural symmetry change defined in Fig. 4. The coefficients \( a, b \) and \( c_{\nu} \) are energies that depend mainly on the respective phonon frequencies and atomic masses. The amplitudes are normalized such that \( \nu_i = 1 \) before arrival of the pump pulse. The double-well potential given by the first two terms in equation (3) accounts for the electronic excitation and for modes that are directly related to the Jahn–Teller distortion: the Jahn–Teller and the breathing mode. The last three terms account for atomic motion coherently excited during the subsequent relaxation process. Identifying \( \gamma_i \) with the primary order parameter for the structural distortion, equation (3) corresponds to the result of Landau theory for a second-order phase transition with \( T/T_c \) substituted by \( n_i/n_c \). This functional form of the potential ensures that at any time \( t \) the minimum of the potential is given for \( \gamma_i = \eta_i (i = 1 \ldots 4) \). The fast change in \( n(t) \) induced by the optical pulse launches the coherent oscillatory atomic motions and \( \gamma_i(t) \rightarrow \eta_i(t) \) for \( t \gg \tau \).

We use equations of motion based on equation (3) to model the structural dynamics and to simulate the diffracted intensities (Supplementary Information). The simulated structural responses of the three reflections in Fig. 2a–c are shown in Fig. 2d–f. Despite the drastic simplifications the main features of the observed rich structural dynamics are well reproduced. In particular, we have neglected the significant resonant enhancement from charge order to the (030) reflection. The good agreement between the measured and simulated response for this reflection is indicative of the intrinsic cooperative charge, orbital and atomic order in this material.

The structural transition observed here within the first few picoseconds does not correspond to the full phase transition from monoclinic P2\(_1\)/m to the orthorhombic Pbnm lattice observed at higher temperatures in equilibrium. Owing to their long-range character the required changes of the unit cell lattice constants and the monoclinic angle to reach the final Pbnm lattice cannot occur on this timescale. It is limited by \( \delta \eta_c \), where \( c_\delta \approx 5 \text{ nm ps}^{-1} \) is the speed of sound and \( \delta \approx 75 \text{ nm} \) (ref. 22) the size of individual domains. Using an average specific heat\(^{23} \) \( c_\delta/T \approx 0.475 \text{ J K}^{-2} \text{ mol}^{-1} \),
resemblance of this description to Landau theory (replacing \(T/T_c\) by \(n/n_c\)) points towards a possible new universal description of complex phase transitions in the time domain. For example, very recently, van Veenendaal has presented a theory of the photoinduced metal–insulator transition in VO\(_2\) in terms of a coherent motion of V–V dimers driven by electronic excitation beyond a certain critical level\(^{16}\). Although this work does not explicitly invoke a time-dependent order parameter \(n_t\) to describe the process, it seems likely that such a description could be made. In general, we would expect that the functional dependence of \(n_t\) could be used for a variety of photoinduced phase transitions in strongly correlated electron systems with coupled electronic and lattice degrees of freedom\(^{13,14}\), but with parameters \(n_\gamma\), \(\gamma\) and \(\tau\) that depend strongly on both the material and the underlying physics of the transition.

### Methods

#### Sample preparation and characterization.

The \((0\overline{1})\)-oriented \(\text{Pr}_2\text{Ca}_5\text{Mn}_3\text{O}_{12}\) thin film of approximately 40 nm thickness was grown on \((0\overline{1})\)-oriented \((\text{LaAlO}_3)_{0.5}(\text{SrAl}_2\text{O}_4)_0.3\) (LSAT) using a pulsed laser deposition technique with a laser pulse frequency of 2 Hz at 850°C in an oxygen pressure of 1.5 mTorr (ref. 22). During the experiment the sample temperature was held at 100 K, well below \(T_{\text{COO}}\approx 220\) K, using a cryogenic nitrogen blower. Static X-ray diffraction experiments to characterize the sample were performed at the X04SA beam line at the Swiss Light Source, Paul Scherrer Institut (Supplementary Information).

#### Time-resolved diffraction experiment.

The experiment was performed at the X-ray Pump–Probe (XPP) instrument at the Linac Coherent Light Source (LCLS) at the SLAC National Accelerator Laboratory\(^{15}\). The experimental set-up is depicted schematically in Fig. 1a. A weakly focused (230 × 230 \(\mu\)m\(^2\)) 55 fs optical pulse with a wavelength of 800 nm excited the sample with a repetition rate of 120 Hz at an incidence angle of 14° (p-polarization). An asymmetric diffraction configuration\(^{10}\) was used to probe the laser-induced structural changes. The horizontally polarized 50 fs X-ray probe pulses were focused to a spot size of \(50 \times 34 \mu\)m\(^2\) and entered the film at 8° grazing incidence. The X-ray energy was tuned in the vicinity of the Mn K edge using a silicon (111) monochromator. The inevitable jitter between pump and probe pulses was measured shot-by-shot using the spectral encoding correlation technique, which has an accuracy of \(\sim 15\) fs (full-width at half-maximum; ref. 28). This information was then used to re-bin the data, significantly improving the time resolution (Supplementary Information).


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**Author contributions**

U.S., S.L.J. and P.B. conceived the experiment; A.C., S.O.M., S.L.J. and U.S. wrote the manuscript with discussions and improvements from all authors.

**Additional information**

Supplementary information is available in the online version of the paper. Reprints and permissions information is available online at www.nature.com/reprints. Additional information and requests for materials should be addressed to P.B.

**Competing financial interests**

The authors declare no competing financial interests.